

SAMPLING

A signal that is bandlimited to a frequency of B Hz can (theoretically) be reproduced exactly from samples taken at a rate of $2B$ Hz or greater.

<p><i>Sampling Theorem:</i></p> $\bar{f}(t) = f(t)\delta_T(t) = \sum_n f(nT)\delta(t - nT)$	<p>$\bar{f}(t)$ is the sampled signal $f(t)$ is the signal $\delta_T(t)$ is the impulse train (regularly spaced pulses of size 1) T is the sampling interval in seconds n is an integer denoting a particular impulse $F_s = 1/T$ is the sampling rate in Hz.</p>
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<p><i>from Dr. Sandberg:</i></p> $\frac{1}{T} f(t) = \sum_{n=-\infty}^{\infty} f(nT) \frac{\sin \bar{w}(t - nT)}{\pi(t - nT)},$ <p>$\omega_0 < 2w$, small ϵ</p>	<p>$f(t)$ is the signal $f(nT)$ is the sampled signal T is the sampling interval in seconds n is an integer denoting a particular impulse t is time in seconds $2w$ is called the Nyquist frequency ϵ is the width of the impulse ω_0 is the radian frequency of the signal</p>
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Aliasing is a type of distortion found in signal sampling which may be viewed in a graph of the signal in the time domain as overlapping tails. It may be eliminated by bandlimiting the signal before sampling.

The **Nyquist interval** is the minimum sampling interval required to recover the original signal from its samples, equal to the reciprocal of twice the bandwidth.

The **Nyquist rate** is the minimum sampling rate required to recover the original signal from its samples, equal to $2\times$ the bandwidth.

The **sinc function**, also known as the filtering or interpolating function is defined as

$$\text{sinc}(x) = \frac{\sin x}{x}.$$